

Contents lists available at ScienceDirect

## Journal of Solid State Chemistry



journal homepage: <www.elsevier.com/locate/jssc>

## Rapid Communication

# Density functional study on electronic and optical properties of C (or N)-doped cubic cerium dioxide

## Yufen Zhang <sup>a,\*</sup>, Xian Zhao <sup>b</sup>

<sup>a</sup> Department of Chemistry and Chemical Technology, Jinan University, Jinan 250022, PR China b State Key Lab of Crystal Materials, Shandong University, Jinan 250100, PR China

#### article info

Article history: Received 14 July 2009 Received in revised form 12 August 2009 Accepted 14 August 2009 Available online 20 August 2009

Keywords: DFT Electronic and optical properties Doping of C (or N) CeO<sub>2</sub>

### 1. Introduction

Lanthanide dioxides ( $LnO<sub>2</sub>$ ) with a cubic fluorite structure have attracted much attention for their wide applications as optical component materials and laser hosts. Out of  $LnO<sub>2</sub>$  type compounds, cubic fluorite ( $Fm3m$ ) cerium dioxide ( $CeO<sub>2</sub>$ ) is well known for the broad applications in automobile exhaust catalysts as oxygen storage, due to its ability to take up and release oxygen under oxidizing and reducing conditions. With a band gap of 3.2 eV and a high UV absorption and a refractive index of 2.35, cubic CeO<sub>2</sub> has been proposed as a potential substitute for TiO<sub>2</sub> and its optical properties has been the focus of intensive research [\[1–9\]](#page-2-0) for recent years. It has been reported that substitutional doping of N (or C) in  $TiO<sub>2</sub>$  has a profound effect on the electronic and optical properties [\[10–13\].](#page-2-0) So it can be speculated that incorporation of low concentrations of N or C impurity in cubic  $CeO<sub>2</sub>$  could induce a different electronic structure and optical properties that may lead to new applications. It is therefore timely to investigate the electronic structure of these systems. For recent years,  $CeO<sub>2</sub>$  based materials have attracted many experimental and theoretical investigations [\[9,14–19\],](#page-2-0) in which, the method of density functional theory (DFT) has been successfully used in predicting crystal structures and properties of  $CeO<sub>2</sub>$  [\[9,14–16\]](#page-2-0). In this paper, we carried out first-principles calculations based on DFT to investigate the electronic structures of the C (or N)-doped cubic CeO<sub>2</sub> (denoted CeO<sub>2</sub>:C or N) and probed the role of anion 2p

### **ABSTRACT**

Density functional calculations were performed on electronic and optical properties of C (or N)-doped cubic cerium dioxide (CeO<sub>2</sub>). When O is replaced by C (or N) in CeO<sub>2</sub>, obvious band-gap ( $E_g$ ) reduction is observed. Meanwhile, it is interesting to find that the substitutional doping of C (or N) in CeO<sub>2</sub> obviously increases the O 2p–Ce 4f transition intensity and also the refractive index. The increase in the O 2p–Ce 4f transition intensity on going from undoped, N-doped and C-doped CeO<sub>2</sub> was related to the covalent character of the Ce–O bond. Compared with the undoped CeO<sub>2</sub>, the C (or N)-doped CeO<sub>2</sub>, with steep absorption peaks at lower energy, can be used for visible-light absorption applications.

 $© 2009$  Elsevier Inc. All rights reserved.

and Ce 4f orbitals in the optical properties, including the optical gap, O 2p–Ce 4f transition intensity and the refractive index. We focus our attention on the trends in the electronic and optical properties of C-doped, N-doped and undoped  $CeO<sub>2</sub>$ . We hope that such calculations could provide more insights into the relation between the structure and the properties for  $CeO<sub>2</sub>$ .

#### 2. Computational method and details

The first-principles electronic structure calculations based on DFT [\[20\]](#page-2-0) within CASTEP 4.1 code [\[21\]](#page-3-0) were carried out to determine the stability and electronic structures of the undoped and  $C$  (or N) doped  $CeO<sub>2</sub>$ . The Vanderbilt ultrasoft pseudopotential [\[22\]](#page-3-0) with generalized gradient approximation due to Perdew Burke Ernzerhof (GGA-PBE) [\[23\]](#page-3-0) for exchange-correlation effects was used to model our systems. A cutoff energy of 410 eV for C (or N) doped and undoped  $CeO<sub>2</sub>$  in the plane wave expansion was employed in the calculations. A  $4 \times 4 \times 4$  Monkhorst–Pack grid [\[24\]](#page-3-0) was used for integration over the irreducible part of the Brillouin zone of the doped and undoped  $CeO<sub>2</sub>$ . Good convergence was achieved with the cutoff energy and number of k points. The default convergence criteria of CASTEP was applied within energy tolerance 5.0e–6 eV/atom, max force tolerance 0.01 eV/ $\AA$ , max displacement tolerance  $5.0e-4\text{ Å}$  and max stress tolerance 0.02 GPa. To explore the electronic and optical properties of these solid solutions, we employed a 96-atoms supercell (containing  $2 \times 2 \times 2$  full cubic cells) with the starting configuration of cubic CeO<sub>2</sub> suggested in Ref. [\[15\].](#page-2-0) We substituted O atoms by C (or N)

<sup>\*</sup> Corresponding author. E-mail address: [yufen720924@126.com \(Y. Zhang\).](mailto:yufen720924@126.com)

<sup>0022-4596/\$ -</sup> see front matter  $\circ$  2009 Elsevier Inc. All rights reserved. doi:[10.1016/j.jssc.2009.08.017](dx.doi.org/10.1016/j.jssc.2009.08.017)

<span id="page-1-0"></span>atoms to model substitutional C or N neutral impurity in  $CeO<sub>2</sub>$ , the resulting supercells are  $Ce_{32}O_{60}C_4$  and  $Ce_{32}O_{60}N_4$ . Within the Broyden–Fletcher–Goldfarb–Shanno (BFGS) scheme [\[25\],](#page-3-0) geometry optimization was performed under Fm3m space group allowing both cell parameter and internal coordinates relaxation. In the electronic and optical property calculation, the underestimation of the band gap (inherent in DFT calculations) was corrected by introducing a "scissors operator" (0.9 eV), by which the conduction band positions were raised in energy prior to the interband transition strength calculation to match the general features of the measured imaginary part of dielectric function [\[9\]](#page-2-0).

### 3. Results and discussions

#### 3.1. Structural stability and population analysis

The calculated equilibrium structural parameters and the results of population analysis of three structures are summarized in Table 1. The calculated equilibrium structural parameter a for  $CeO<sub>2</sub>$  is 5.464 Å, which is in good agreement with the experimental value of 5.416Å [\[26\].](#page-3-0) This can demonstrate the applicability of our theoretical model in geometry optimization for  $CeO<sub>2</sub>$ . For  $CeO<sub>2</sub>$ : C (or N), the equilibrium structural parameters a is  $\sim$ 5% (or 2%) larger than CeO<sub>2</sub>.

From the results of population analysis, it is clear to find that substitutional doping of C (or N) will not change the Mulliken charge of O atoms, but obviously lower the charge of Ce atoms, because C (or N) is more likely to donate electron to Ce than O atoms. The bond order between a pair of atoms is a measure of the strength of the bond. It can be calculated from the overlap integrals between the Bloch functions with an atomic basis expansion [\[27\].](#page-3-0) The total bond order of a crystal can be obtained by multiplying the individual bond order by the number of bonds per molecular unit. In Table 1, it is interesting to find that the Mulliken bond order for Ce–C is  $\sim 0.16$  (bond length = 2.434 Å) obviously decrease, for Ce–N  $\sim$ 0.23 (2.396Å) slightly increase than Ce–O  $\sim$ 0.21 (2.366 Å), and the total bond order both for Cdoped (6.74) and for N-doped CeO<sub>2</sub> (6.92) obviously increase, compared with undoped system (6.72). The amazing part is that in going from  $CeO<sub>2</sub>:C$  (or N) to  $CeO<sub>2</sub>$ , the total 30  $Ce-O$  bond order are actually increased by  $\sim$ 1.9 (or  $\sim$ 2.5)%. So it can be predicted that  $CeO<sub>2</sub>:C$  (or N) is much more covalent than  $CeO<sub>2</sub>$ .

#### 3.2. Electronic properties

Fig. 1 shows the calculated density of states (DOS) of the C-doped, N-doped and undoped CeO<sub>2</sub> 96-atoms supercell. In

#### Table 1

Calculated equilibrium structural parameters and the results of population analysis of three structures.





Fig. 1. DOS of (a) C-doped; (b) N-doped and (c) undoped  $CeO<sub>2</sub>$ .



Fig. 2. PDOS of (a) C-doped and (b) N-doped  $CeO<sub>2</sub>$ .

Fig. 2, we plot the total DOS (TDOS) and partial DOS (PDOS) spectra of both C-doped and N-doped structures. In Figs. 1 and 2, the Fermi energy  $(E_f)$  locates at  $\sim$ 0 eV for both undoped and N-doped CeO<sub>2</sub>, for C-doped CeO<sub>2</sub>  $E_f = \sim -0.9$  eV. For the doped systems, the C (or N) concentration is 6.25%, which results from substituting four O atoms with four C (or N) atoms in a 96-atoms supercell. There is only one anion site in  $c$ -CeO<sub>2</sub>, so substituting O atom with C (or N) needs not consider the site preference. When O is replaced by C (or N) in CeO<sub>2</sub>, a bandgap ( $E_g$ ) reduction is observed. For  $CeO<sub>2</sub>:C$  (Fig. 1a), an impurity band is clearly found in the band gap. In the case of  $CeO<sub>2</sub>$ :N (Fig. 1b), an obvious increase at the top of valence band makes the width of valence band broaden.

From the result of Figs. 1 and 2, it is found that the valence band is mainly composed of O 2p orbitals and the conduction band of mainly from the contribution of Ce 5d orbitals is located at 5.38, 4.91 and 6.18 eV, above the valence band for C-doped, Ndoped and undoped  $CeO<sub>2</sub>$ , respectively. Between valence band and conduction band, the Ce 4f-block band is located at 1.73, 1.21 and 2.45 eV, above the top of the O 2p-block bands in C-doped, Ndoped and undoped  $CeO<sub>2</sub>$ . For C-doped system (Fig. 2a), the impurity band in the band gap originates from the  $C$  2p orbitals, which are the only state mainly located at the impurity band. In Fig. 2b, the increase of TDOS at the top of valence band for  $CeO<sub>2</sub>$ :N is introduced by the N impurity, because the N 2p orbitals are the only states mainly located at the valence band maximum.

The width of valence band varies from 4.0 to 4.5 to 4.1 eV on going from C-doped, N-doped and undoped  $CeO<sub>2</sub>$ . The valence band is higher in energy for C-doped CeO<sub>2</sub>, but lower for N-doped

<span id="page-2-0"></span>

Fig. 3. Real and imaginary part of dielectric functions of three structures.

 $CeO<sub>2</sub>$  than for undoped  $CeO<sub>2</sub>$ . The bottom of conduction band is higher in energy for both C-doped and N-doped  $CeO<sub>2</sub>$  than for undoped  $CeO<sub>2</sub>$ . The width of the Ce 4f-block band increases from 1.2 to 1.4 to 1.5 eV on going from undoped, N-doped and C-doped systems. The position of the Ce 4f-block band obviously shifts to lower energy for both C-doped and N-doped  $CeO<sub>2</sub>$ . These may reflect the stronger mixing between Ce 4f–C (or N) 2p than Ce 4f– O 2p orbitals, which may be the reason to cause the O  $2p$ –Ce 4f gap and also the band gap reduction. [Fig. 2](#page-1-0) clearly shows a substantial obvious mixing between Ce 4f and anion 2p orbitals.

#### 3.3. Dielectric constants

The optical properties of C-doped, N-doped and undoped  $CeO<sub>2</sub>$ were also calculated. For all the three systems, the calculated dielectric functions, including the real part  $\varepsilon_1$  and imaginary part  $\varepsilon_2$ , were calculated up to 30 eV and shown in Fig. 3.

The static dielectric constant  $\varepsilon(0)$  is obtained as the zero frequency limit of the real part of the frequency-dependent dielectric function. The calculated  $\varepsilon(0)$  is 3.74 for undoped, 5.11 for N-doped and 6.28 for C-doped CeO<sub>2</sub>. Both C-doped and N-doped  $CeO<sub>2</sub>$  are larger than undoped system. A larger  $\varepsilon(0)$  means a larger refractive index [\[27\].](#page-3-0) From a chemical point of view, the refractive index of a compound is a measure of its polarizability [9]. The C (or N)-doped  $CeO<sub>2</sub>$  are more covalent than the undoped system, so the overall covalent character is stronger in C (or N)-doped systems than in undoped system. Thus, the polarizability and hence the refractive index should be higher in C (or N)-doped systems. A higher optical density for the C (or N)-doped  $CeO<sub>2</sub>$  may have special applications in certain optical components.

In Fig. 3c, the  $\varepsilon_2$  plot for undoped CeO<sub>2</sub> exhibits one major absorption peak at 3.17 eV, which is associated with the O 2p–Ce 4f transition [9]. For C-doped system (Fig. 3a), the  $\varepsilon_2$  plot exhibits three major absorption peaks at 0.9, 2.3 and 3.6 eV, respectively. In Fig. 3b, the  $\varepsilon_2$  plot for N-doped system also exhibits three major absorption peaks at 0.9, 2.9 and 3.7 eV, respectively. It is clear that the dielectric functions of C (or N)-doped CeO<sub>2</sub> are quite different from those of the undoped system. The splitting of the absorption peak in C (or N)-doped CeO<sub>2</sub> should be attributed to the effect of the impurity band introduced by C (or N) atoms. From the results of Fig. 3, it can be found that  $CeO<sub>2</sub>$  present a proper absorption edge for an UV absorber and can be used for UV absorption applications, with a steep absorption peak at the absorption edge  $\sim$ 3.2 eV, which is in good agreement with the results of Goubin et al. [9]. The C (or N)-doped CeO<sub>2</sub>, with steep absorption peaks at lower energy region  $\sim 0.9$ –2.9 eV, can be used for visible-light absorption applications.

From the  $\varepsilon_2$  curves of C (or N)-doped CeO<sub>2</sub>, it is also clear that the absorption intensity associated with the O 2p–Ce 4f transition increases on going from undoped, N-doped and C-doped  $CeO<sub>2</sub>$ . Compared with undoped  $c$ -CeO<sub>2</sub>, the C (or N)-doped system has more extended major absorption region. These observations can be understood by comparing the Ce 4f surroundings. Each Ce atom is surrounded by eight O atoms in  $c$ -CeO<sub>2</sub>. The O 2p–Ce 4f transition is associated essentially with the electron excitation from the 2p orbitals of eight Ce-connected O atoms to the Ce 4f orbitals. Due to the increasing donating electrons ability on going from O, N and C atoms, the O 2p–Ce 4f transition intensity should increase on going from undoped, N-doped and C-doped systems. This can be explained by the increasing covalent character of the Ce–O bond on going from undoped and C (N)-doped CeO<sub>2</sub> with increasing total bond order (presented in [Table 1](#page-1-0)).

In summary, by first-principles pseudopotential calculations, it is predicted that the substitutional doping of C (or N) in cubic CeO<sub>2</sub> lowers the  $E_g$  and also O 2p–Ce 4f gap, and increases the O 2p–Ce 4f transition intensity and also the refractive index. The optical gap is associated with the O 2p–Ce 4f excitation and is influenced by the local environments of Ce atom. An increase in the covalent character of the C (or N)-doped  $CeO<sub>2</sub>$  lowers the O 2p–Ce  $4f$  excitation gap. The increase in the O 2p–Ce  $4f$  transition intensity on going from undoped, N-doped and C-doped  $CeO<sub>2</sub>$  was related to the covalent character of the Ce–O bond. Compared with undoped  $CeO<sub>2</sub>$ , the C (or N)-doped  $CeO<sub>2</sub>$ , with steep absorption peaks at lower energy, can be used for visible-light absorption applications.

#### Acknowledgments

This work was supported by the National Natural Science Foundation of China (NSFC, no. 20473046), Research Program of Ministry of science and Technology (2005CCA00900).

#### Reference

- [1] T. Yamamoto, H. Momida, T. Hamada, T. Uda, T. Ohno, Thin Solid Films 486 (2005) 136.
- [2] M. Marabelli, P. Wachter, Phys. Rev. B 36 (1987) 1238.
- [3] S. Guo, H. Arwin, S.N. Jacobsen, K. Jarrendahl, U. Helmersson, J. Appl. Phys. 77 ¨ (1995) 5369.
- [4] M. Niwano, S. Sato, T. Koide, T. Shidara, A. Fujimori, H. Fukutani, S. Shin, M. Ishigame, J. Phys. Soc. Jpn. 57 (1988) 1489.
- [5] M. Veszelei, L. Kullman, C.G. Granqvist, N. Rottkay, M. Rubin, Appl. Opt. 37 (1998) 5993.
- [6] M. Miyauchi, A. Nakajima, T. Watanabe, K. Hashimoto, Chem. Mater. 14 (2002) 2812–2816.
- [7] M. Primet, E. Garbowski, in: A. Trovarelli (Ed.), Catalysts by Ceria and Related Materials, Imperial College Press, London, 2002, p. 407.
- [8] S. Yabe, M. Yamashita, M. Shigeyosi, T. Kazuyuki, S. Yoshida, R. Li, T. Sato, Int. J. Inorg. Mater. 3 (2001) 1003–1008.
- [9] F. Goubin, X. Rocquefelte, M.-H. Whangbo, Y. Montardi, R. Brec, S. Jobic, Chem. Mater. 16 (2004) 662–669.
- [10] R. Asahi, T. Morikawa, T. Ohwaki, K. Aoki, Y. Taga, Science 293 (2001) 269–271.
- [11] S.U.M. Khan, M. Al-Shahry, W.B. Ingler Jr., Science 297 (2002) 2243–2245.
- J. Graciani, Y. Ortega, J.F. Sanz, Chem. Mater. 21 (2009) 1431-1438
- [13] A. Enrique, R. Garcia, Y. Sun, K.R. Reyes-Gil, D. Raftery, Solid State Nucl. Magn. Reson. 35 (2009) 74–81.
- [14] N.V. Skorodumova, R. Ahuja, S.I. Simak, I.A. Abrikosov, B. Johansson, B.I. Lundqvist, Phys. Rev. B 64 (2001) 115108.
- S. Mehrotra, P. Sharma, M. Rajagopalan, A.K. Bandyopadhyay, Solid State Commun. 140 (2006) 313–317.
- [16] S. Fabris, S. de Gironcoli, S. Baroni, G. Vicario, G. Balducci, Phys. Rev. B 71 (2005) 041102.
- [17] E. Voloshina, B. Paulus, J. Chem. Phys. 124 (2005) 234711.
- [18] C.J. Mao, Y.X. Zhao, X.F. Qiu, J.J. Zhu, C. Burda, Phys. Chem. Chem. Phys. 10 (2008) 5633–5638.
- [19] S.D. Carolis, J.L. Pascual, L.G.M. Pettersson, M. Baudin, M. Wo'jcik, K. Hermansson, A.E.C. Palmqvist, M. Muhammed, J. Phys. Chem. B 103 (1999) 7627–7636.
- [20] W. Kohn, L.J. Sham, Phys. Rev. 140 (1965) A1133.
- <span id="page-3-0"></span>[21] M.C. Payne, M.P. Teter, D.C. Allan, T.A. Arias, J.D. Joannopoulos, Rev. Mod. Phys. 64 (1992) 1045.<br>[22] D. Vanderbilt, Phys. Rev. B 41 (1990) 7892.<br>[23] J.P. Perdew, K. Burke, M. Ernzerhof, Phys. Rev. Lett. 77 (1996) 3865–3868.<br>[24] H.J. Monkhorst, J.D. Pack, Phys. Rev. B 13 (1976) 5188.
- 
- 
- 
- [25] E. Polak, Computational Methods in Optimization, Academic, New York, 1971, p. 56. [26] S.J. Duclos, Y.K. Vohra, A.L. Ruoff, A. Jayaraman, G.P. Espinosa, Phys. Rev. B 38 (1988) 7755.
- [27] S.-D. Mo, L. Ouyang, W.Y. Ching, I. Tanaka, Y. Komyama, R. Riedel, Phys. Rev. Lett. 83 (1999) 5046.